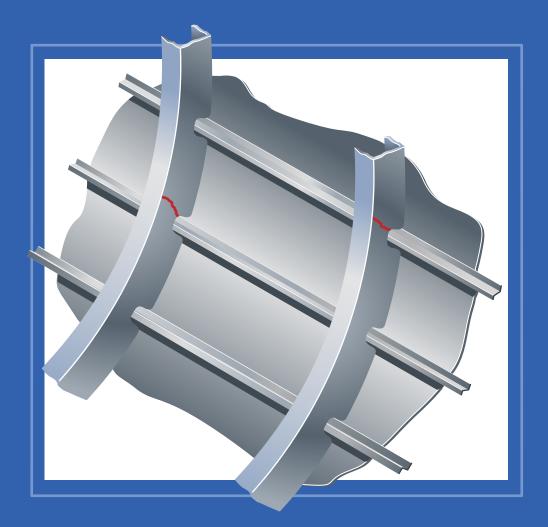
# Practical Airframe Fatigue and Damage Tolerance



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Fracture mechanics in complex geometry/stress fields using boundary element and finite element analysis.

## PRACTICAL AIRFRAME FATIGUE AND DAMAGE TOLERANCE

by

Les Bent

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